## APPENDIX:

## ADDITIONAL DETAILS OF THE REPORTED SPECIFICATIONS

(The tables show estimated standard errors in parentheses and probability values in square brackets.)

## CONSTANT NATURAL RATE SPECIFICATION

Table A1:

| Size and Significance of Coefficient on $\mathbf{u}_{t-1}$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| USA | Canada | Japan | Germany | France | Italy | UK |  |
| -0.135 | -0.060 | -0.120 | -0.021 | -0.030 | -0.051 | -0.030 |  |
| $(0.035)$ | $(0.186)$ | $(0.123)$ | $(0.014)$ | $(0.013)$ | $(0.028)$ | $(0.023)$ |  |

TWO KNOT CUBIC SPLINE NATURAL RATE SPECIFICATION
Table A2:

| Size and Significance of Coefficient on $\mathrm{u}_{\mathrm{t}-1}$ |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| USA | Canada | Japan | Germany | France | Italy | UK |
| $\begin{gathered} -0.364 \\ (0.063) \end{gathered}$ | $\begin{aligned} & -0.195 \\ & (0.043) \end{aligned}$ | $\begin{aligned} & -0.944 \\ & (0.444) \end{aligned}$ | $\begin{aligned} & -0.242 \\ & (0.055) \end{aligned}$ | $\begin{aligned} & -0.224 \\ & (0.099) \end{aligned}$ | $\begin{gathered} 0.024 \\ (0.113) \end{gathered}$ | $\begin{aligned} & -0.147 \\ & (0.072) \end{aligned}$ |
| Significance of Spline Regressors |  |  |  |  |  |  |
| USA | Canada | Japan | Germany | France | Italy | UK |
| $F(5,109)$ | $F(5,108)$ | $F(5,107)$ | F(5,111) | $F(5,108)$ | $F(5,108)$ | $F(5,106)$ |
| 4.22 [.002] | 2.22 [.057] | 1.11[.361] | 4.25[.001] | 6.05[.000] | 2.67[.026] | 0.72[.610] |

Table A3:

Significance of Deterministic Functions of Time, $\mathrm{P}(\mathrm{t})$

| USA <br> 2 Knot Cubic <br> Spline | Canada <br> Quadratic Trend | Japan <br> Quadratic Trend | Germany <br> Linear <br> Trend | France <br> Linear <br> Trend | Italy <br> Linear <br> Trend | UK <br> Mean Shift <br> in 1980:2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $F(5,109) 4.2[.00]$ | $F(2,111) 4.7[.01]$ | $F(2,110) 2.1[.13]$ | t -stat. $3.71[.00]$ | t -stat. $2.40[.02]$ | t -stat. 1.47[.14] | t -stat 3.07[.00] |

Size and Significance of Coefficient on $\mathrm{u}_{\mathrm{t}-1}$

| $\begin{aligned} & -0.364 \\ & (0.063) \end{aligned}$ | $\begin{aligned} & -0.193 \\ & (0.039) \\ & \hline \end{aligned}$ | $\begin{aligned} & -0.588 \\ & (0.261) \end{aligned}$ | $\begin{aligned} & -0.162 \\ & (0.042) \end{aligned}$ | $\begin{aligned} & -0.224 \\ & (0.055) \end{aligned}$ | $\begin{aligned} & -0.161 \\ & (0.070) \end{aligned}$ | $\begin{aligned} & -0.187 \\ & (0.053) \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Joint Significance of $\Delta \mathrm{u}$ terms |  |  |  |  |  |  |
| F(1,109)17.0[.00] | $F(1,110) 5.4[.02]$ | none | none | none | none | F(1,111)12.4[.00] |
| Joint Significance of $\Delta^{2} \mathrm{p}$ terms |  |  |  |  |  |  |
| F(5,109) 24.0[.00] | F(5,110) 15.5[.00] | F(5,110) 20.1[.00] | F(4,115) 14.7.00] | F( 2,114 ) 19.5[.00] | F(5,112) 42.9[.00] | F( 5,111 ) 26.7[.00] |
| Equation Standard Error and Sample Standard Deviation of $\Delta^{2} p$ |  |  |  |  |  |  |
| 0.4610 | 0.4878 | 0.8038 | 0.4325 | 0.6878 | 0.7772 | 0.8656 |
| 0.7599 | 0.7289 | 1.4412 | 0.5718 | 0.4809 | 1.3780 | 1.5881 |

Table A4:

| Diagnostic Test Probability Values |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | USA | Canada | Japan | Germany | France | Italy | UK |
| Normality | 0.501 | 0.618 | 0.847 | 0.875 | 0.193 | 0.882 | 0.371 |
| LM1 | 0.596 | 0.219 | 0.632 | 0.802 | 0.316 | 0.324 | 0.108 |
| LM4 | 0.547 | 0.264 | 0.206 | 0.975 | 0.185 | 0.626 | 0.301 |
| LM8 | 0.110 | 0.267 | 0.427 | 0.707 | 0.295 | 0.183 | 0.212 |
| Heteroscedasticity | 0.014 | 0.574 | 0.889 | 0.341 | 0.464 | 0.794 | 0.364 |
| ARCH1 | 0.402 | 0.353 | 0.105 | 0.851 | 0.029 | 0.089 | 0.519 |
| ARCH4 | 0.589 | 0.219 | 0.378 | 0.778 | 0.185 | 0.117 | 0.001 |
| Ramsey Reset | 0.186 | 0.250 | 0.944 | 0.171 | 0.920 | 0.063 | 0.348 |

Table A5:
TESTS OF PREFERRED SPECIFICATIONS OF TIME VARYING NATURAL RATES AGAINST ALTERNATIVES

| USA: Preferred Specification-2 Knot Cubic Spline |  |  |
| :---: | :---: | :---: |
| Rival Specification | Test Statistic | Interpretation |
| trend | $\mathrm{F}(4,109)=5.21$ [.001] | reduction to trend specification is rejected |
| quadratic | $F(3,109)=4.02$ [.009] | reduction to quadratic specification is rejected |
| cubic | $F(2,109)=5.71$ [.004] | reduction to cubic specification is rejected |
| 1 knot cubic spline | $F(2,108)=3.09$ [.050] | raising 1 to 2 knots is not rejected at 5\% level |
| 3 knot cubic spline | $F(3,106)=1.21$ [.309] | extra regressors for 3 knot spline are jointly insignificant |
| Canada: Preferred Specification - Quadratic Trend |  |  |
| Rival Specification | Test Statistic | Interpretation |
| trend | $F(1,110)=4.35$ [.039] | reduction to trend specification is rejected |
| cubic | $F(1,109)=1.79$ [.183] | extra regressor for cubic is insignificant |
| 1 knot cubic spline | $F(2,108)=1.36$ [.262] | extra regressors for 1 knot spline are jointly insignificant |
| 2 knot cubic spline | $F(3,107)=1.18$ [.320] | extra regressors for 2 knot spline are jointly insignificant |
| 3 knot cubic spline | $\mathrm{F}(4,106)=1.43$ [.230] | extra regressors for 3 knot spline are jointly insignificant |
| BZ mean shift | $F(3,107)=0.98$ [.406] | additional mean shifts are jointly insignificant |
| Japan: Preferred Specification - Quadratic Trend |  |  |
| Rival Specification | Test Statistic | Interpretation |
| trend | $F(1,110)=1.99$ [.162] | reduction to trend specification cannot be rejected |
| cubic | $F(1,109)=0.01[.943]$ | extra regressor for cubic is insignificant |
| 1 knot cubic spline | $F(2,108)=0.00$ [.997] | extra regressors for 1 knot spline are jointly insignificant |
| 2 knot cubic spline | $F(3,107)=0.48$ [.698] | extra regressors for 2 knot spline are jointly insignificant |
| 3 knot cubic spline | $\mathrm{F}(4,106)=0.77$ [.545] | extra regressors for 3 knot spline are jointly insignificant |
| BZ mean shift | $\mathrm{F}(4,106)=1.61$ [.177] | additional mean shifts are jointly insignificant |
| Germany: Preferred Specification - Linear Trend |  |  |
| Rival Specification | Test Statistic | Interpretation |
| quadratic | t-statistic . 208 [.84] | raise to quadratic specification is rejected |
| cubic | $F(2,113)=2.66[.07]$ | extra cubic regressor is not rejected at 7\% significance level |
| 1 knot cubic spline | $F(3,112)=2.00[.12]$ | extra regressors for 1 knot cubic spline are jointly insignificant |
| 2 knot cubic spline | $F(4,111)=1.79$ [.14] | extra regressors for 1 knot cubic spline are jointly insignificant |
| 3 knot cubic spline | $F(5,110)=1.76[.13]$ | extra regressors for 1 knot cubic spline are jointly insignificant |

France: Preferred Specification - Linear Trend

| Rival Specification | Test Statistic | Interpretation |
| :---: | :---: | :---: |
| quadratic | t-statistic 0.10 [.92] | raise to quadratic specification is rejected |
| cubic | $F(2,112)=0.50[.61]$ | extra regressors for cubic spline are jointly insignificant |
| 1 knot cubic spline | $F(3,111)=0.50[.68]$ | extra regressors for 1 knot cubic spline are jointly insignificant |
| 2 knot cubic spline | $F(4,110)=0.49$ [.79] | extra regressors for 1 knot cubic spline are jointly insignificant |
| 3 knot cubic spline | $F(5,109)=0.49$ [.79] | extra regressors for 1 knot cubic spline are jointly insignificant |
| UK: Preferred Specification - Mean Shift |  |  |
| Rival Specification | Test Statistic | Interpretation |
| trend | t-statistic 0.99 [.32] | addition of a linear trend term is rejected |
| quadratic | $F(2,109)=1.69$ [.14] | quadratic terms in T are jointly insignificant |
| cubic | $F(3,108)=2.62[.05]$ | cubic terms in T are jointly insignificant at the 5\% significance level |
| 1 knot cubic spline | $F(4,107)=1.98$ [.10] | 1 knot cubic spline regressors are jointly insignificant |
| 2 knot cubic spline | $F(5,106)=1.69$ [.14] | 2 knot cubic spline regressors are jointly insignificant |
| 3 knot cubic spline | $F(6,105)=1.47$ [.20] | 3 knot cubic spline regressors are jointly insignificant |

