# **APPENDIX:**

ADDITIONAL DETAILS OF THE REPORTED SPECIFICATIONS (The tables show estimated standard errors in parentheses and probability values in square brackets.)

#### **CONSTANT NATURAL RATE SPECIFICATION**

#### Table A1:

Size and Significance of Coefficient on $u_{t-1}$						
USA	Canada	Japan	Germany	France	Italy	UK
-0.135 (0.035)	-0.060 (0.186)	-0.120 (0.123)	-0.021 (0.014)	-0.030 (0.013)	-0.051 (0.028)	-0.030 (0.023)

#### TWO KNOT CUBIC SPLINE NATURAL RATE SPECIFICATION

#### Table A2:

Size and Significance of Coefficient on ut-1						
USA	Canada	Japan	Germany	France	Italy	UK
-0.364 (0.063)	-0.195 (0.043)	-0.944 (0.444)	-0.242 (0.055)	-0.224 (0.099)	0.024 (0.113)	-0.147 (0.072)
Significance of Spline Regressors						
USA	Canada	Japan	Germany	France	Italy	UK
F(5,109)	F(5,108)	F(5,107)	F(5,111)	F(5,108)	F(5,108)	F(5,106)
4.22 [.002]	2.22 [.057]	1.11[.361]	4.25[.001]	6.05[.000]	2.67[.026]	0.72[.610]

# PREFERRED SPECIFICATIONS OF TIME VARYING NATURAL RATES

### Table A3:

Significance of Deterministic Functions of Time, P(t)							
USA 2 Knot Cubic Spline	Canada Quadratic Trend	Japan Quadratic Trend	Germany France Linear Linear Trend Trend		Italy Linear Trend	UK Mean Shift in 1980:2	
F(5,109) 4.2[.00]	F(2,111) 4.7[.01]	F(2,110) 2.1[.13]	,110) 2.1[.13] t-stat. 3.71 [.00] t-stat. 2.40 [.02]		t-stat. 1.47 [.14]	t-stat 3.07 [.00]	
	Size and Significance of Coefficient on u <sub>t-1</sub>						
-0.364 (0.063)	-0.193 -0.588 (0.039) (0.261)		-0.162 (0.042)	-0.162 -0.224 (0.042) (0.055)		-0.187 (0.053)	
Joint Significance of $\Delta u$ terms							
F(1,109)17.0[.00]	F(1,110) 5.4[.02] none		none	none	none	F(1,111)12.4[.00]	
Joint Significance of $\Delta^2 p$ terms							
F(5,109) 24.0[.00]	F(5,109) 24.0[.00] F(5,110) 15.5[.00] F(5,110) 20.1[.00]		F(4,115) 14.7[.00] F(2,114) 19.5[.00]		F(5,112) 42.9[.00]	F(5,111) 26.7[.00]	
Equation Standard Error and Sample Standard Deviation of $\Delta^2 p$							
0.4610 0.7599	0.4878 0.7289	0.8038 1.4412	0.4325 0.5718	0.6878 0.4809	0.7772 1.3780	0.8656 1.5881	

# Table A4:

Diagnostic Test Probability Values							
	USA	Canada	Japan	Germany	France	Italy	UK
Normality	0.501	0.618	0.847	0.875	0.193	0.882	0.371
LM1	0.596	0.219	0.632	0.802	0.316	0.324	0.108
LM4	0.547	0.264	0.206	0.975	0.185	0.626	0.301
LM8	0.110	0.267	0.427	0.707	0.295	0.183	0.212
Heteroscedasticity	0.014	0.574	0.889	0.341	0.464	0.794	0.364
ARCH1	0.402	0.353	0.105	0.851	0.029	0.089	0.519
ARCH4	0.589	0.219	0.378	0.778	0.185	0.117	0.001
Ramsey Reset	0.186	0.250	0.944	0.171	0.920	0.063	0.348

# TESTS OF PREFERRED SPECIFICATIONS OF TIME VARYING NATURAL RATES AGAINST ALTERNATIVES

USA: Preferred Specification - 2 Knot Cubic Spline						
Rival Specification	Test Statistic	Interpretation				
trend	F(4,109)=5.21 [.001]	reduction to trend specification is rejected				
quadratic	F(3,109)=4.02 [.009]	reduction to guadratic specification is rejected				
cubic	F(2,109)=5.71 [.004]	reduction to cubic specification is rejected				
1 knot cubic spline	F(2,108)=3.09 [.050]	raising 1 to 2 knots is not rejected at 5% level				
3 knot cubic spline	F(3,106)=1.21 [.309]	extra regressors for 3 knot spline are jointly insignificant				
	Canada: Preferre	ed Specification - Quadratic Trend				
Rival Specification	Test Statistic	Interpretation				
trend	F(1,110)=4.35 [.039]	reduction to trend specification is rejected				
cubic	F(1,109)=1.79 [.183]	extra regressor for cubic is insignificant				
1 knot cubic spline	F(2,108)=1.36 [.262]	extra regressors for 1 knot spline are jointly insignificant				
2 knot cubic spline	F(3,107)=1.18 [.320]	extra regressors for 2 knot spline are jointly insignificant				
3 knot cubic spline	F(4,106)=1.43 [.230]	extra regressors for 3 knot spline are jointly insignificant				
BZ mean shift	F(3,107)=0.98 [.406]	additional mean shifts are jointly insignificant				
	Japan: Preferred	d Specification - Quadratic Trend				
Rival Specification	Test Statistic	Interpretation				
trend	F(1,110)=1.99 [.162]	reduction to trend specification cannot be rejected				
cubic	F(1,109)=0.01 [.943]	extra regressor for cubic is insignificant				
1 knot cubic spline	F(2,108)=0.00 [.997]	extra regressors for 1 knot spline are jointly insignificant				
2 knot cubic spline	F(3,107)=0.48 [.698]	extra regressors for 2 knot spline are jointly insignificant				
3 knot cubic spline	F(4,106)=0.77 [.545]	extra regressors for 3 knot spline are jointly insignificant				
BZ mean shift	F(4,106)=1.61 [.177]	additional mean shifts are jointly insignificant				
	Germany: Preferred Specification - Linear Trend					
Rival Specification	Test Statistic	Interpretation				
quadratic	t-statistic .208 [.84]	raise to quadratic specification is rejected				
cubic	F(2,113)=2.66 [.07]	extra cubic regressor is not rejected at 7% significance level				
1 knot cubic spline	F(3,112)=2.00 [.12]	extra regressors for 1 knot cubic spline are jointly insignificant				
2 knot cubic spline	F(4,111)=1.79 [.14]	extra regressors for 1 knot cubic spline are jointly insignificant				
3 knot cubic spline	F(5,110)=1.76 [.13]	extra regressors for 1 knot cubic spline are jointly insignificant				
	France: Prefer	red Specification - Linear Trend				
Rival Specification	Test Statistic	Interpretation				
quadratic	t-statistic 0.10 [.92]	raise to quadratic specification is rejected				
cubic	F(2,112) =0.50 [.61]	extra regressors for cubic spline are jointly insignificant				
1 knot cubic spline	F(3,111) =0.50 [.68]	extra regressors for 1 knot cubic spline are jointly insignificant				
2 knot cubic spline	F(4,110) =0.49 [.79]	extra regressors for 1 knot cubic spline are jointly insignificant				
3 knot cubic spline	F(5,109) =0.49 [.79]	extra regressors for 1 knot cubic spline are jointly insignificant				
UK: Preferred Specification - Mean Shift						
Rival Specification	Test Statistic	Interpretation				
trend	t-statistic 0.99 [.32]	addition of a linear trend term is rejected				
quadratic	F(2,109) =1.69 [.14]	quadratic terms in T are jointly insignificant				
cubic	F(3,108) =2.62 [.05]	cubic terms in T are jointly insignificant at the 5% significance level				
1 knot cubic spline	F(4,107) =1.98 [.10]	1 knot cubic spline regressors are jointly insignificant				
2 knot cubic spline	F(5,106) =1.69 [.14]	2 knot cubic spline regressors are jointly insignificant				
3 knot cubic spline	F(6,105) =1.47 [.20]	3 knot cubic spline regressors are jointly insignificant				